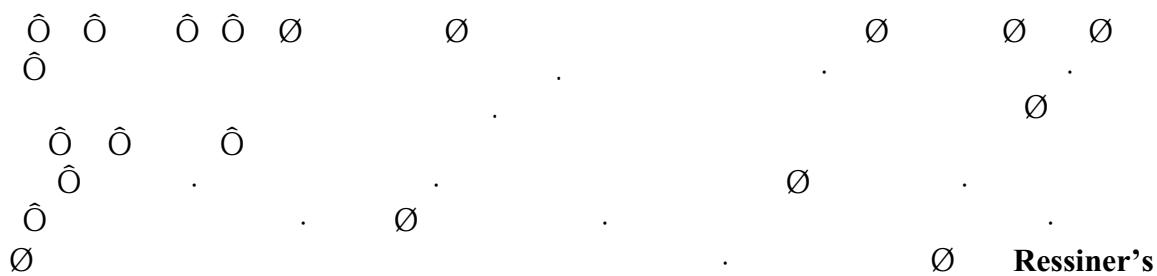


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EFFECT OF CYCLIC HEATING ON REINFORCED CONCRETE THICK PLATES

Dr. AH AHMAD *

H.M.A. HASAN **

ABSTRACT

The aim of this investigation is to study the effect of cyclic heating and cooling on the nonlinear analysis of the reinforced concrete plate at different load conditions before and after cracking up to failure, and it's effect on cracking and crushing of concrete and yielding of steel. Also to calculate the stresses and strains due to the applied load under the effect of cyclic heating and cooling.

The study also present the mathematical mode for the behavior of the reinforced concrete plate under cyclic heating with different variables , such as temperatures , duration of heating, and number of cyclic heating ,The relation between load and deflection .is presented .

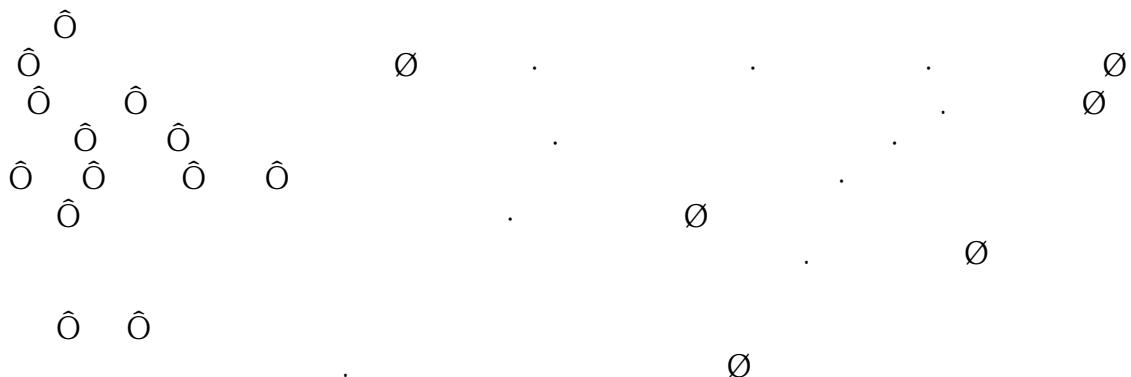
Ressiner's theory has been used to represent the behavior of thick plate . The Finite Difference method and Dynamic Relaxation have been used in the solution of the differential equations ..

* Professor , Civil Engineering Dept.

** MSc. Graduate .

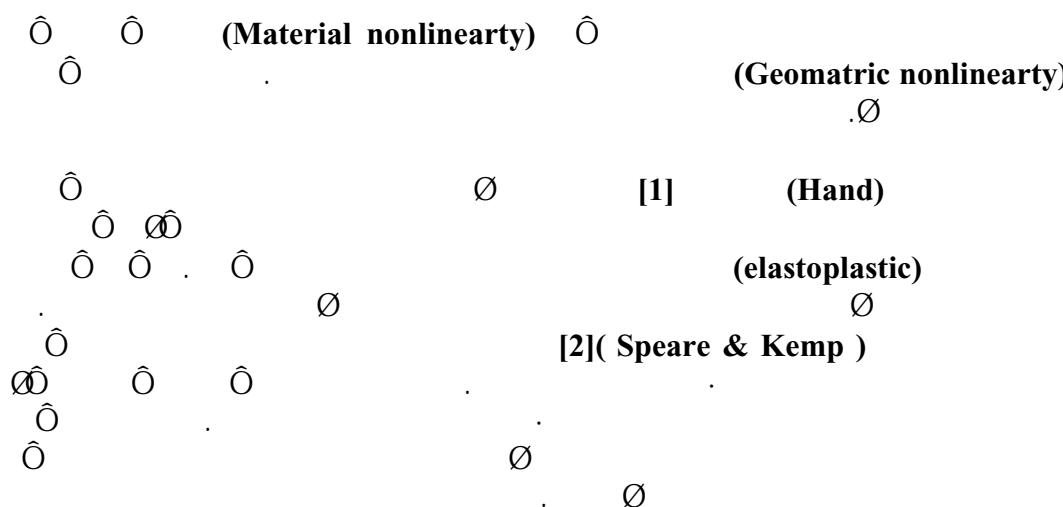
Introduction

- 1



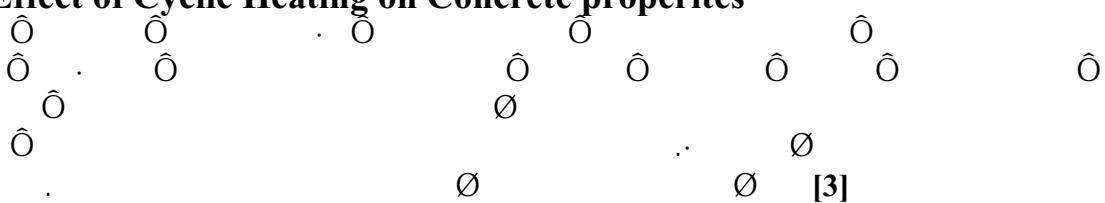
Nonlinear behavior of Plates

1.1



- 1.2

Effect of Cyclic Heating on Concrete properties



1.3

Concrete Members Subjected to High Temperatures

∅ [4] Khan & Royles
(20-800)°C

Effect of High Temperature no the Reinforcing Bars During Heating and After Cooling

[6] Homles
O O . (20-700)°C . Ø
O O O O
Ø Ø

| | | | | | | |
|--------------|------------|--------------|------------|------------|----------------|----------------|
| O | O | O | O | O | O | [8] |
| O | O | | | | 476 MPa | 345 MPa |
| O | O | 500°C | | | \emptyset | |
| 700°C | 70% | | | 89% | | 600°C |

S420M - (400-700)°C [9] Mäkeläinen (stress-strain)

Materials Constitutive Relationship-

-2

2.1

Ultimate Strength of Concrete under Biaxial Compression

| [10] Liu | $\sigma_p / \sigma_{\circ T}$ | α | σ_p |
|-------------|-----------------------------------|----------------------------|--------------------|
| \emptyset | $1 + \frac{\alpha}{1.2 - \alpha}$ | $\alpha < 0.2$ | $\sigma_{\circ T}$ |
| \emptyset | 1.2 | $0.2 \leq \alpha \leq 1.0$ | $\sigma_{\circ T}$ |
| \emptyset | $\frac{1.2}{\alpha}$ | $1.0 \leq \alpha \leq 5.0$ | $\sigma_{\circ T}$ |
| \emptyset | $1 + \frac{1}{1.2\alpha - 1}$ | $\alpha > 5.0$ | $\sigma_{\circ T}$ |

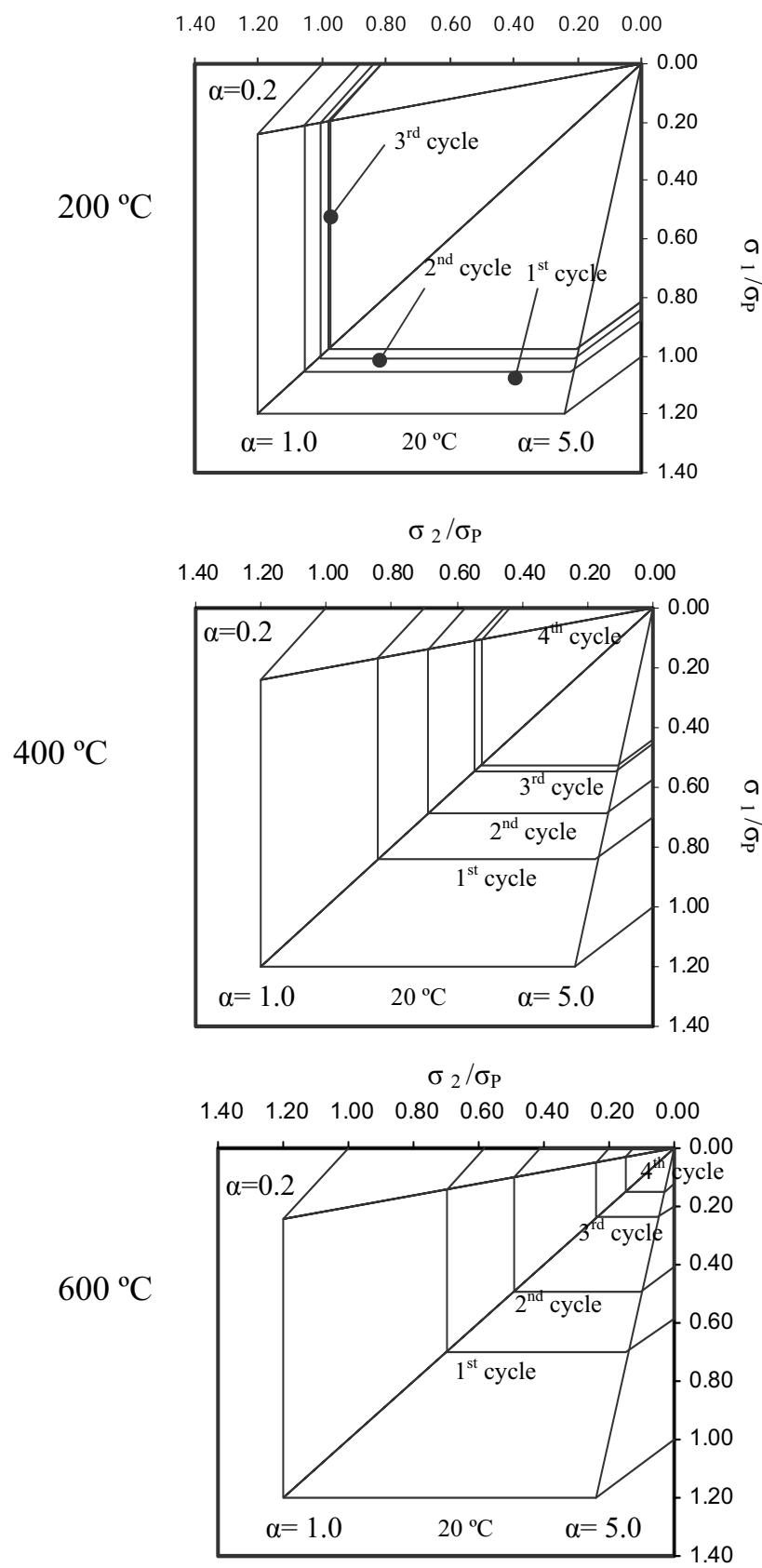
Strain at Ultimate Biaxial Compression Stress

$$\hat{O} \quad [10] \text{ Liu} \quad \emptyset \quad : \quad \emptyset \\ \varepsilon_p = -2500 \times 10^{-6} \quad (\text{Major Direction}) \quad (2)$$

$$\varepsilon_p = -0.0025 \times \xi \quad (\text{Major Direction}) \dots \quad (4)$$

$$\varepsilon_p = (500 + \xi_1 \cdot \sigma_p) \times 10^{-6} \quad (\text{Minor Direction}) \dots \quad (5)$$

$$\xi_1 = 0.0266(500 + \varepsilon_p(\text{major}) \times 10^6)$$



∅ (1) ∅

Concrete Under Biaxial Tension and Tension Compression Cases

$$\begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \tau_{12} \end{bmatrix} = \begin{bmatrix} \lambda' E_{lb}' / E_{2b}' & \lambda' v_1 & 0 \\ \lambda' v_1 & \lambda' & 0 \\ 0 & 0 & E_{lb}' E_{2b}' / (E_{lb}' + E_{2b}' + 2E_{2b}' v_2) \end{bmatrix} \begin{Bmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \gamma_{12} \end{Bmatrix}$$

$$\begin{bmatrix} \tau_{13} \\ \tau_{23} \end{bmatrix} = \begin{bmatrix} E_{lb}' E_C / (E_{lb}' + E_C + 2E_C v_1) & 0 \\ 0 & E_{2b}' E_C / (E_{2b}' + E_C + 2E_C v_2) \end{bmatrix} \begin{Bmatrix} \gamma_{13} \\ \gamma_{23} \end{Bmatrix} \quad(7)$$

$$E_{1b}' = \frac{E \left[1 - (\varepsilon_1 / \varepsilon_p)^2 \right]}{\left[1 + \left(\frac{E}{E_s(1-v\alpha)} - 2 \right) \left(\frac{\varepsilon_1}{\varepsilon_p} \right) + \left(\frac{\varepsilon_1}{\varepsilon_p} \right)^2 \right]^2} \quad \dots \dots \dots (8)$$

$$E_{2b} = \frac{E[1 - (\varepsilon_2/\varepsilon_p)^2]}{\left[1 + \left(\frac{E}{E_s(1-\nu\alpha)} - 2\right)\left(\frac{\varepsilon_2}{\varepsilon_p}\right) + \left(\frac{\varepsilon_2}{\varepsilon_p}\right)^2\right]^2} \quad \dots \dots \dots (9)$$

$$E'_{1b} = E'_{2b} = E \quad \text{uniaxial modulus of elasticity} \quad \dots \dots \dots \quad (10)$$

$$\lambda' = E_{1b}' / (E_{1b}' / E_{2b} - v^2) \quad : \quad \emptyset \quad - \quad 2-4$$

Stress-Strain Relations for Cracked Concrete

$$\begin{array}{ccc}
 \hat{\emptyset} & \emptyset & \cdot \\
 \emptyset & \emptyset & \cdot \\
 & & : \\
 & & \emptyset - \\
 \left[\begin{array}{c} \sigma_1 \\ \sigma_2 \\ \tau_{12} \\ \tau_{13} \\ \tau_{23} \end{array} \right] = \left[\begin{array}{ccccc} 0 & 0 & 0 & 0 & 0 \\ 0 & C_1 E & 0 & 0 & 0 \\ 0 & 0 & G_{12} & 0 & 0 \\ 0 & 0 & 0 & G_{13} & 0 \\ 0 & 0 & 0 & 0 & G_{23} \end{array} \right] \left[\begin{array}{c} \varepsilon_1 \\ \varepsilon_2 \\ \gamma_{12} \\ \gamma_{13} \\ \gamma_{23} \end{array} \right] & \dots & (11) \\
 & & \emptyset \quad (1) \emptyset
 \end{array}$$

| | | | | |
|-----------------|-----------------|-----------------|-----------------|----------------------|
| \hat{O} | (C) | \cdot | \emptyset | $(C=1.0)$ |
| \hat{O} | $\hat{\otimes}$ | $[1,13,14]$ | $\hat{\otimes}$ | $\emptyset : G_{ij}$ |
| \hat{O} | \cdot | \cdot | \hat{O} | \hat{O} |
| $G_{12} = 0.4G$ | $G_{13} = 0.4G$ | $G_{23} = G$ | \vdots | (1) |
| $G_{12} = 0.4G$ | $G_{13} = G$ | $G_{23} = 0.4G$ | \vdots | (2) |
| $G_{12} = 0.4G$ | $G_{13} = 0.4G$ | $G_{23} = 0.4G$ | \vdots | |

Tension Stiffening

$$\sigma = \frac{\alpha_2 \alpha_2 f_t'}{1 + \sqrt{500 \varepsilon_i}} \quad . \quad \begin{array}{c} \varepsilon_i > \varepsilon_{cr} \\ \emptyset \end{array} \quad : \quad \varepsilon_{cr} \quad (12)$$

| | | | |
|-----------------------|-------------|-------------|------------------|
| (Deformed Bar) | \emptyset | \emptyset | $\alpha_1 = 1.0$ |
| | | \emptyset | $\alpha_1 = 0.7$ |

$$(\alpha_2 = 0.7)$$

$$\begin{array}{c} \textcircled{O} \quad \textcircled{O} \quad \textcircled{\times} \\ \textcircled{O} \quad \textcircled{\times} \\ (\mathbf{c/d}) \quad \textcircled{O} \quad \textcircled{O} \quad \textcircled{O} \end{array} \quad (\alpha_3) \quad \emptyset \quad [12] \text{ (Abrishami \& Mitchell)} \\ \quad : \quad \emptyset \quad (12)$$

$$\sigma_t = \frac{\alpha_1 \alpha_2 \alpha_3 f_t}{1 + \sqrt{500 \varepsilon_i}} \quad (13)$$

$$\alpha_3 = 1.0$$

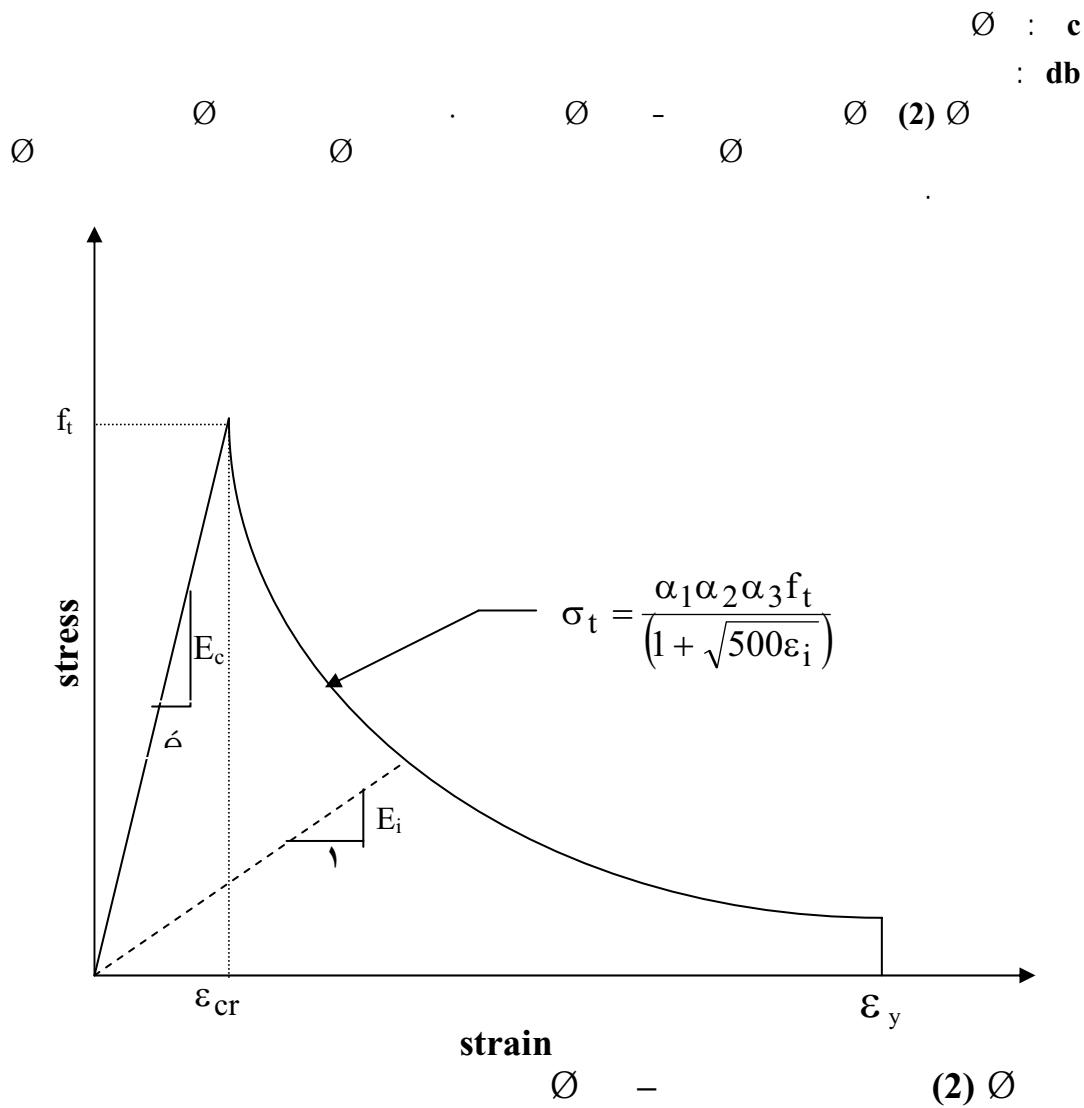
for $c/d_b > 2.5$

$$\alpha_3 = 0.8(c/d_b) - 1$$

for $1.25 \leq c/d_b \leq 2.5$

$$\alpha_3 = 0.0$$

for $c/d_b < 1.25$



Behavior of Steel Reinforced

-2.6

| | | | | |
|------------------|-------------------|--------------|-------------|------------------|
| \hat{O} | \hat{O} | \emptyset | \emptyset | \emptyset |
| $\hat{O}\hat{O}$ | . (3) \emptyset | [6] (Homles) | \emptyset | .(4) \emptyset |

Method of Analysis

- طريقة التحليل 3

õ ù
õ õ ù ù ù

$$-\frac{\partial^2 \bar{M}_x}{\partial \bar{x}^2} - 2 \frac{\partial^2 \bar{M}_{xy}}{\partial \bar{x} \partial \bar{y}} - \frac{\partial^2 \bar{M}_y}{\partial \bar{y}^2} + \bar{D}_f \frac{\partial \bar{\omega}}{\partial \bar{t}} + \bar{m} \frac{\partial^2 \bar{\omega}}{\partial \bar{t}^2} = \bar{q} \quad \dots \dots \dots (14)$$

$$\bar{\omega}_{(i)j}^{\circ} = \frac{1}{1+0.5\bar{D}_v} \left[(1-0.5\bar{D}_v)\bar{\omega}_{(i)j-1}^{\circ} + \frac{\Delta t}{m} \left(\frac{\partial^2 \bar{M}_x}{\partial x^2} \right)_i + 2 \left(\frac{\partial^2 \bar{M}_{xy}}{\partial x \partial y} \right)_i + \left(\frac{\partial^2 \bar{M}_y}{\partial y^2} \right) + \bar{q}_i \right] \quad (15)$$

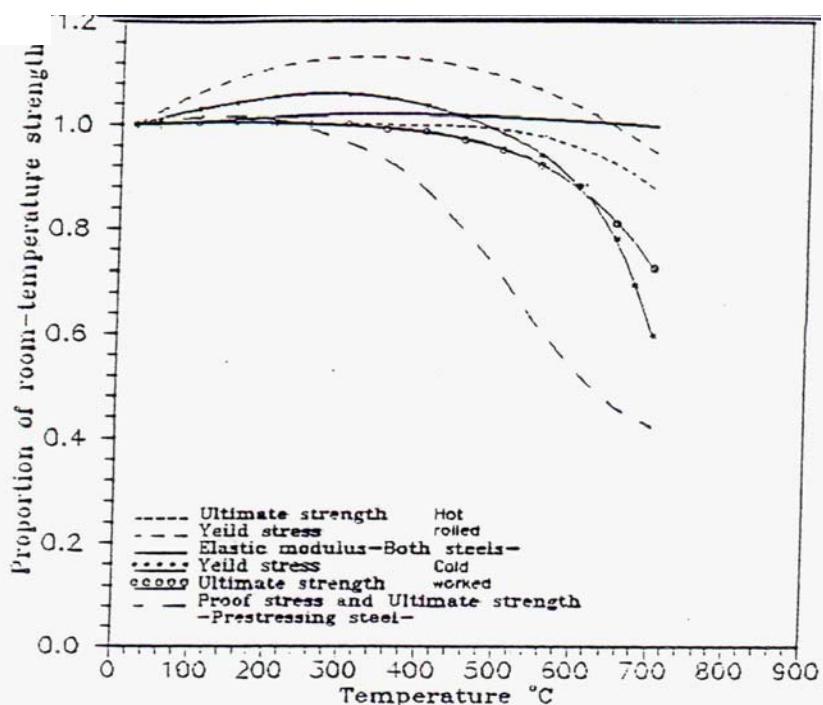
$$\sum_{k=1}^{k=j+0.5} \bar{\omega}_{(i)k} = \sum_{k=1}^{k=j-0.5} \bar{\omega}_{(i)k} + \bar{\omega}_{(i)j}^{\circ} \Delta t \quad \dots \quad (16)$$

$$D_v = \frac{\bar{D}_f \Delta t}{m} \quad U$$

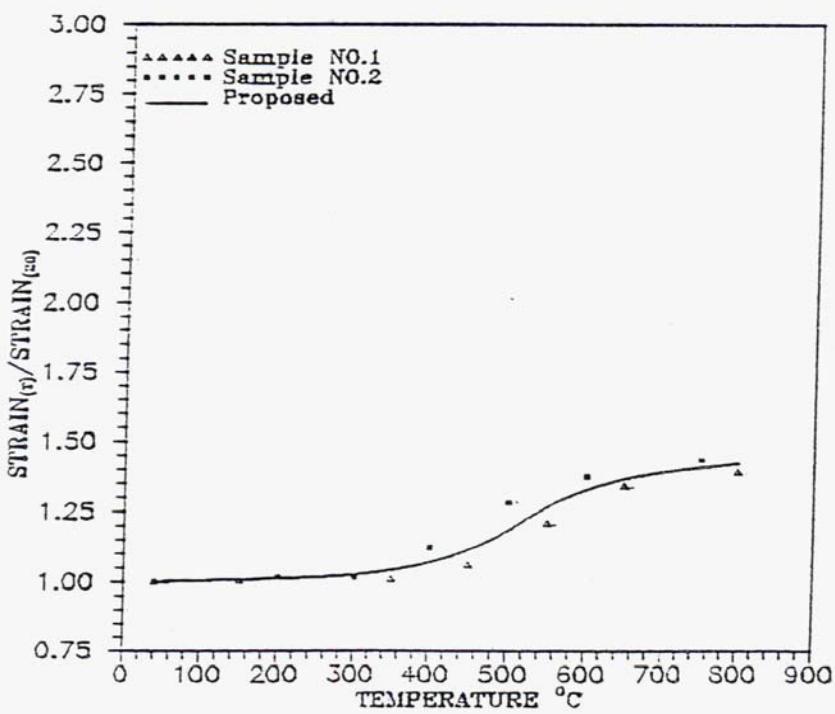
1

: j

: ω



شكل (13.5) تغير خواص أنواع مختلفة من حديد التسليح بعد الدورة الأولى من التسخين



الشكل (14.5) تغير إنفعال الخضوع في الحديد بعد الدورة الأولى من التسخين .

$$\left. \begin{array}{l} \omega = 0 \\ M_x = 0 \\ \phi_y = 0 \end{array} \right\} \quad \text{أما محددات الإسناد لصفحة بسيطة بالإسناد فهي كما يلي :} \quad x \text{ is constant} \quad \dots \dots \dots \quad (17)$$

Ó Ú , Ú , (Plan Stress)
 Ó Ú Ó Ó Ú . Ú
 Ó Ó , Ú .

Nonlinear Analysis Methods

-4

تم استخدام الطريقة المعدلة للزيادات المحددة التي تعتمد على $D_{av} = \frac{D_1 + D_2}{2}$. ومن ثم تحسب قيمة معدل الجسامة المماسية كما يلي :

Results and Discussion

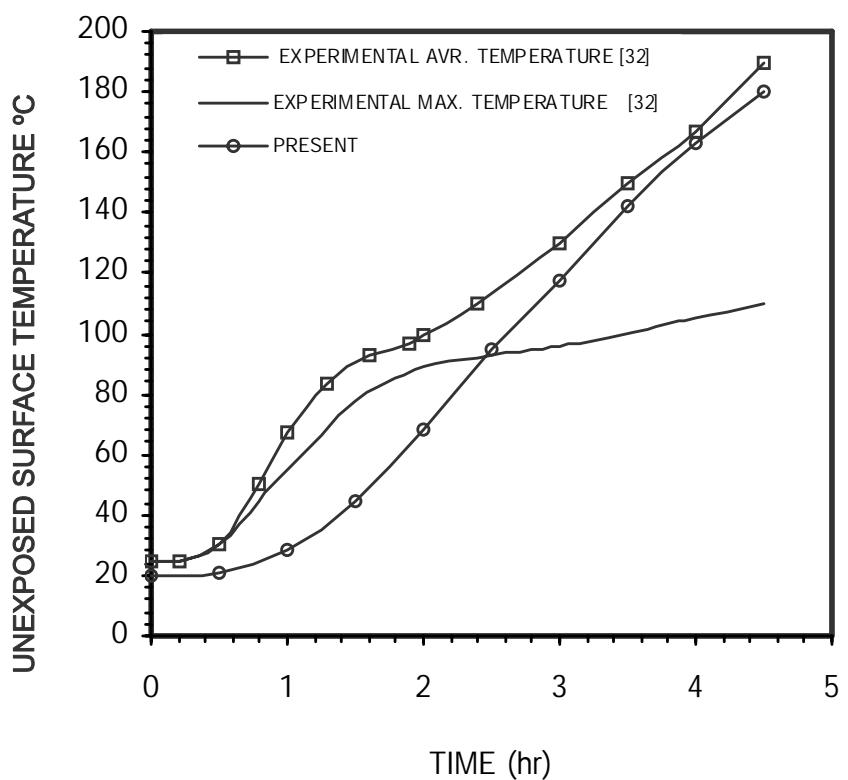
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Thermal diffusing

1-5

Ó Ó Ó Ó Ú
 (2375 kg/m³) (177.8mm) Ó Ó Ó ,
 - : (ISO 834)
 .1.3 W/m.C° Ú Ú
 .850 J/kg.C°

Ó Ó (5) Ù
[14] Ù
Ó Ó Ù
Ù Ù
Ù Ù

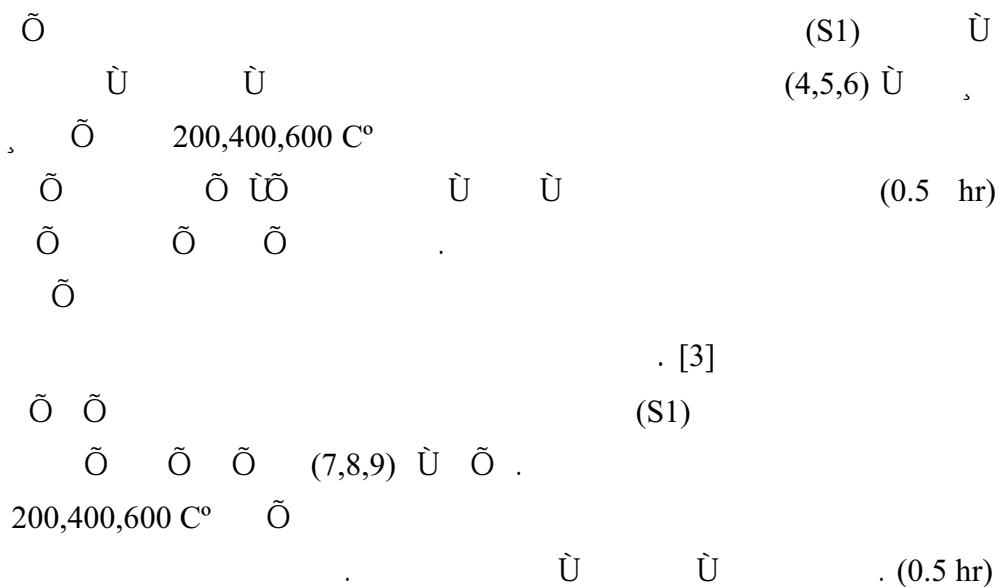


(5) Ø

(ISO 834)

Structural Analysis

Ø 2-5



Conclusions

.6

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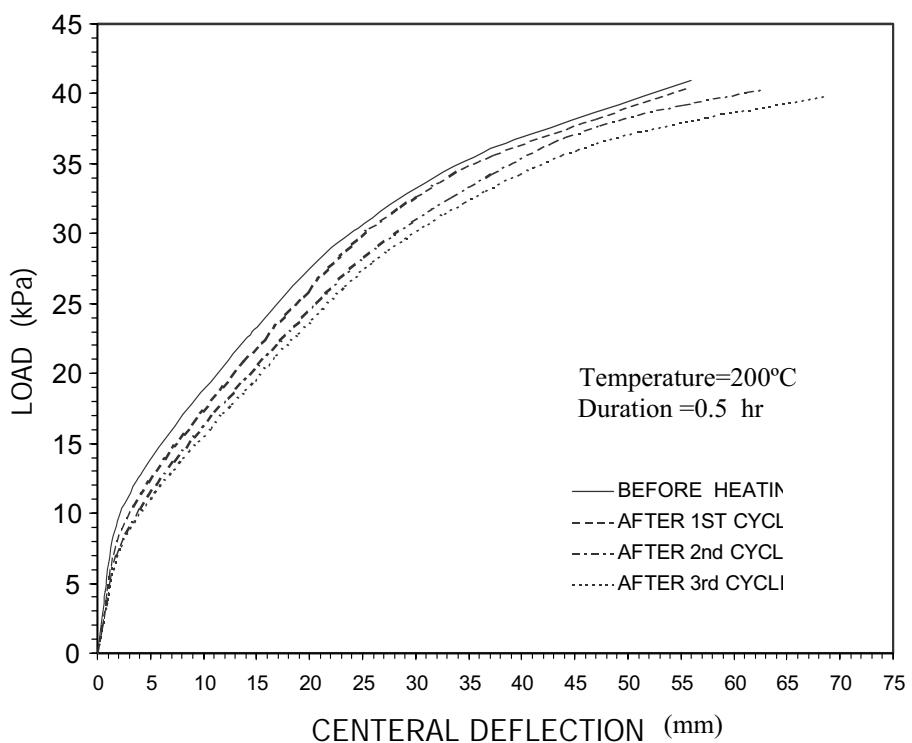
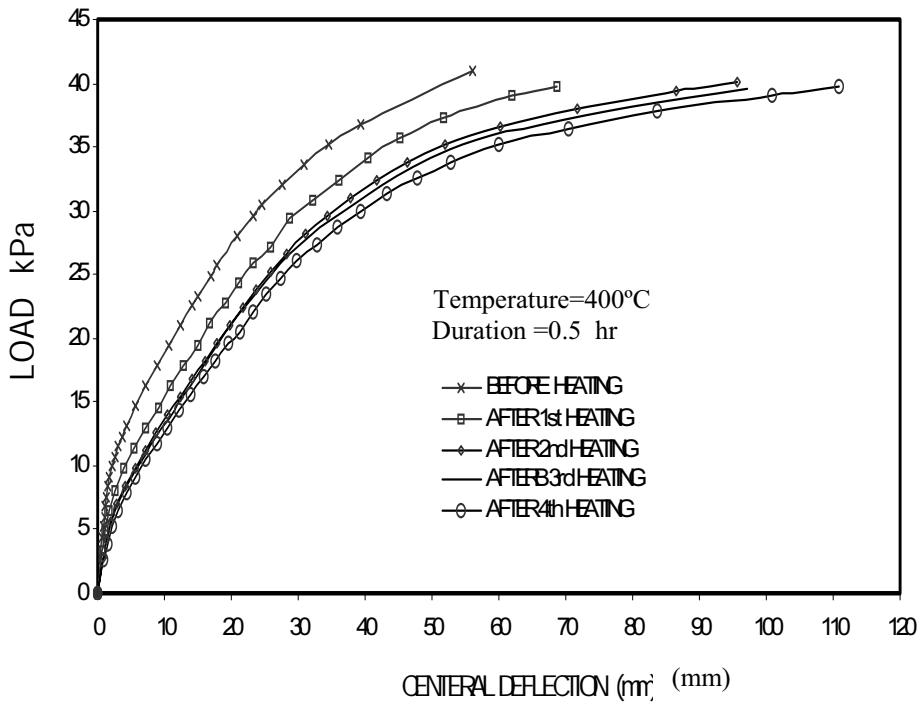
الحرارة العالية " ،

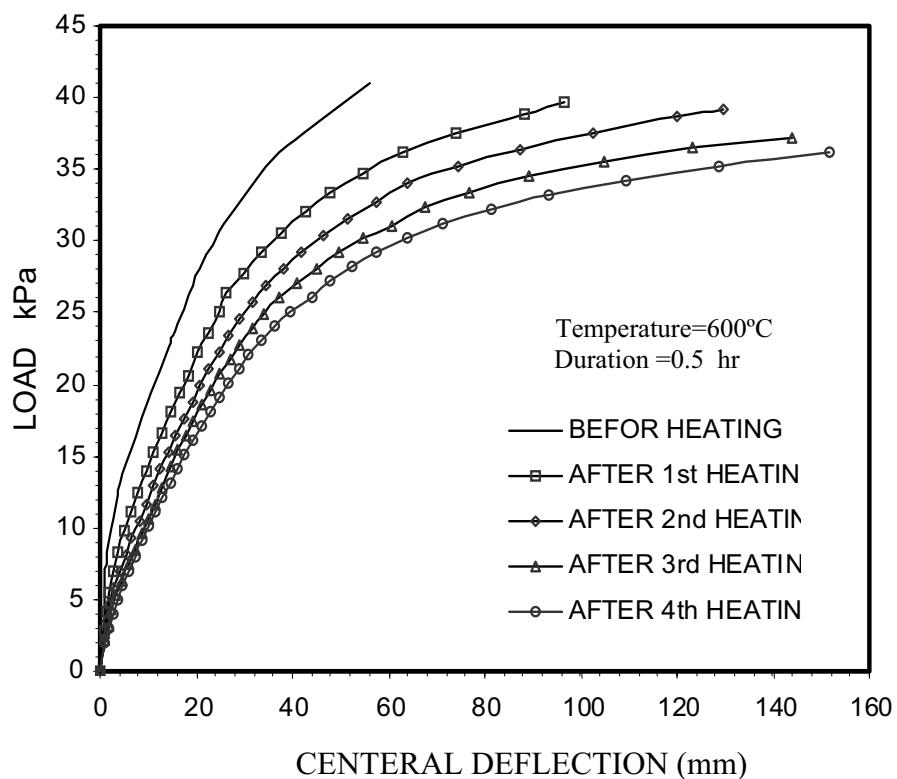
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**200°C****(S1)****-Ø****(4) Ø****400°C****(S1)****Ø****(5) Ø**

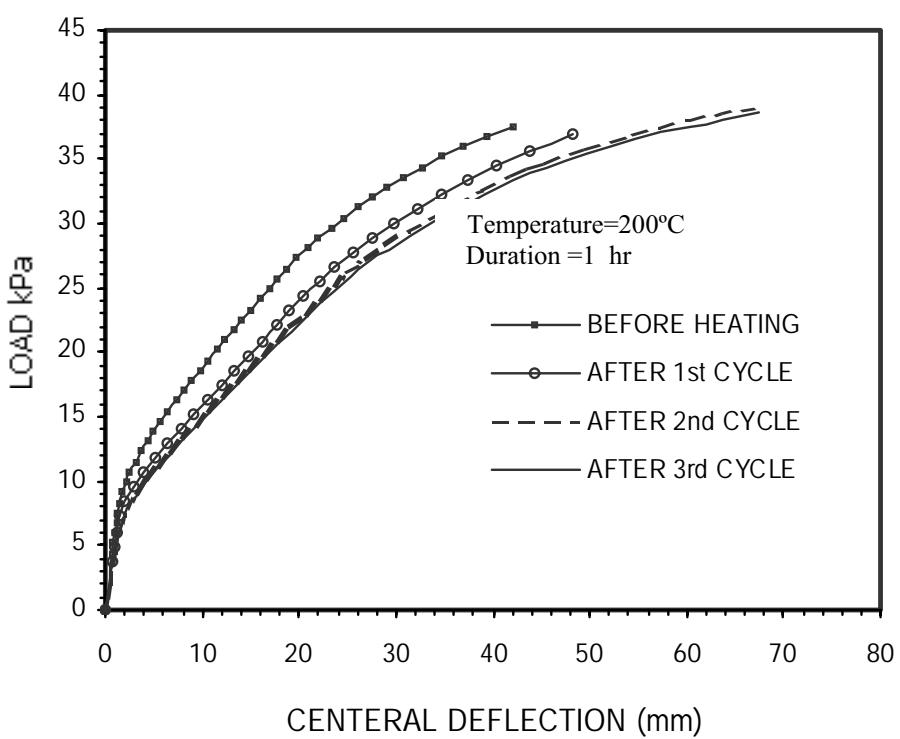


600°C

(S1)

\emptyset

(6)Ø



200°C

(S1)

\emptyset

(7) Ø

