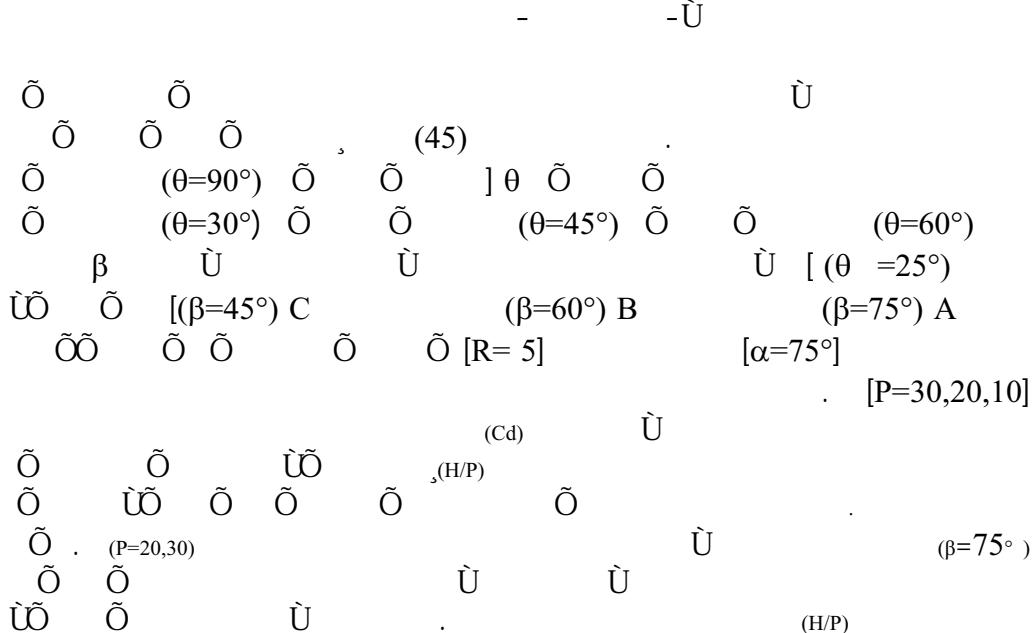


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## Coefficient of Discharge For the Normal and Oblique Weirs with Semi-Circular Crest

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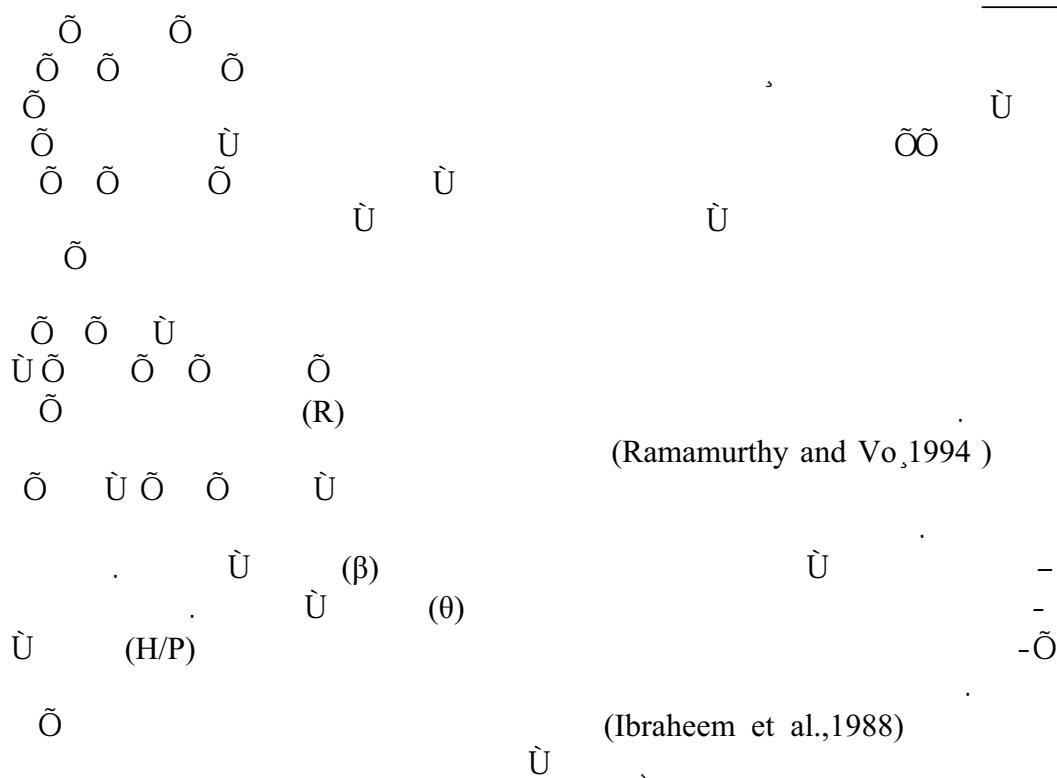
### ABSTRACT

The coefficient of discharge of normal and oblique weirs with semicircular crest under free over flow conditions was studied experimentally. Forty-five weir models were constructed and tested. These models classified in to five groups based on the variation of oblique angle with the canal wall ( $\theta$ )[group one ( $\theta=90^\circ$ ), group two ( $\theta=60^\circ$ ), group three ( $\theta=45^\circ$ ), group four ( $\theta=30^\circ$ ), group five ( $\theta=25^\circ$ )]. Each group included three series of tests depending on the variation of downstream face slope ( $\beta$ )[series A ( $\beta=75^\circ$ ), series B ( $\beta=60^\circ$ ), series C ( $\beta=45^\circ$ )]. The upstream slop was fixed for all models with angle ( $\alpha =75^\circ$ ) and the crest radius ( $R=5$  cm). Every series included testing of three models based on the variation of weir height [ $P=30,20\&10$  cm].

The experimental results of the study showed that the discharge coefficient ( $C_d$ ) increases with the increase of water depth above the crest to the weir height ratio( $H/P$ ), and with the increase of downstream slope( $\beta$ ) the peak values of ( $C_d$ ) were found when downstream face slope ( $\beta=75^\circ$ ) and weir height ( $P=10$  cm). In case of oblique weirs, it was found that ( $C_d$ ) decreases with increase of ( $H/P$ ) values. Also it was found that ( $C_d$ ) increases with the increase of the downstream slope ( $\beta$ ) & weirs of small oblique angle ( $\theta$ ) give low values of ( $C_d$ ).

**Keywords:** Weirs; Free-fall Structures Experimental Study

$$\begin{aligned}
 \hat{U} &= C_d \\
 \hat{U} &= g \\
 &= h \\
 \hat{U} &= L \\
 &= P \\
 &= Q_{NC} \\
 &= Q_{NS} \\
 &= Q_{OB} \\
 &= R \\
 &= Re \\
 &= V \\
 &= B \\
 &= \mu \\
 &= \rho \\
 &= \theta \\
 \hat{U} &= \alpha \\
 \hat{U} &= \beta \\
 &= f, f_1, f_2
 \end{aligned}$$



$\tilde{O}$ $\tilde{U}$	( Abid Ali, 1989)
$\tilde{O}$ $\tilde{U}$	( Ramamurthy and Vo, 1994)
$\tilde{O}$ $\tilde{U}\tilde{O}$ $(\beta=45^\circ)$	$\tilde{U}$ $(\alpha=90^\circ)$
$\tilde{O}$ $\tilde{U}\tilde{O}$ $(C_d)$	$\tilde{U}$ $(H/R=3)$ $(C_d)$
$\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{U}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$ $(H/R>3)$ $(5.5)$
$\tilde{U}\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $(D/R)$ $\tilde{O}$	$\tilde{U}$ $(H/R>3)$ $(C_d)$
$\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$ $(H/R>3)$ $(Chanson \text{ and } Montes, 1998)$
$\tilde{U}\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$ $(Ziba Vatannia, 1999)$
$\tilde{O}$ $\tilde{U}$ $(H/P)$	$\tilde{U}$ $(AL-Humaidawa, 2000)$
$\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$ $(\theta)$ $\tilde{U}$ $(C_d)$ $(Al-Tikriti, R., 2000)$
$\tilde{O}$ $\tilde{U}$	$\tilde{U}$
$\tilde{U}\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$ $(Abdel-Azim M. Negm et al., 2002)$
$\tilde{O}$ $\tilde{O}$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$
$\tilde{O}$ $(\tilde{O} \tilde{O})$ $\tilde{O}$ $\tilde{O}$	$\tilde{U}$ $(45)$ $\tilde{U}$ $(45)$ $(1)$ $\tilde{U}$
$\tilde{O}(\theta) \tilde{O} \tilde{O} \tilde{O} \tilde{O}$ $\tilde{O} \quad (\theta=45^\circ) \tilde{O}$	$\tilde{U}$ $(\theta=60^\circ)$ $\tilde{U}$ $(\theta=90^\circ)$ $(5)$
	$\emptyset$

O [ (θ = 25°) , (θ = 30°) ]  
 (β = 60°) B O , (β = 75°) A ] , (β ) U [ (β = 45°) C  
 [α = 75°] U U U [ R = 5 ]  
 (1) U O (P = 30, 20, 10) O U (2) U

U (315) . (B.S.I 1965) OOOO  
 . (White 1977) ( ) (2.5) U (7)  
 U .(Q<sub>NC</sub>) (40)  
 .(H) U  
 .(Rehbock) OOO (P) U  
 (Q<sub>NS</sub>)

$$Q_{NS} = \frac{2}{3} C_d \sqrt{2g} L H_e^{1.5} \quad \dots \dots \dots \quad (1)$$

$$C_d = (0.602 + 0.083 \frac{H}{P})$$

$$H_e = (H + 0.0012)$$

$$\begin{array}{c} \text{.}(\text{ / }) \\ \text{.}(\text{ )} \\ \vdots \end{array} \quad \begin{array}{c} =Q_{NS} \\ =P \\ \mathbf{\hat{U}} \end{array}$$

$$.( / ) = Q_{NC}$$

∅

$$f(q, H, P, g, \rho, \mu, \beta, \theta) = 0 \quad \dots \dots \dots \quad (3)$$

$$\frac{(L^3/T \cdot L)}{(L)} = \frac{U}{(L/T^2)} = q = H$$

U :

$$\begin{array}{lll}
 (M/T^3) & & = \rho \\
 \tilde{O} & = \mu \\
 \tilde{U} & = (M/T \cdot L) \beta \\
 & = \theta
 \end{array}$$

[(pie-Theorem)  $\Rightarrow$   $\exists$   $\hat{U}$   $\cup$   $(q, H, \mu)$  .]

$$\frac{Q_{NC}}{\frac{2}{3} * \sqrt{2g} * B^* H^{3/2}} = C_d = f_l \left( \frac{H}{P}, Re, \beta, \theta \right) \dots \dots \dots (4)$$

$$\begin{array}{ccccc} \textcircled{O} & \textcircled{O} & \textcircled{O} & (\text{Re}) & (4) \\ \textcircled{O} & \textcircled{U} & & & \textcircled{U} \end{array}$$

$$\begin{array}{cccccc} & & & & \emptyset & \\ \vdots & & (\mathbf{C}_d) & \emptyset & \emptyset & -\mathbf{1} \end{array}$$

$\tilde{U}$   
 $\tilde{W}$        $\tilde{O}$        $\tilde{O}$        $\tilde{O}$        $\tilde{O}$        $\tilde{O}$        $\tilde{O}$        $(C_d)$   
 $\tilde{W}$        $\tilde{O}$        $(5,4,3,8,9,7,6)$        $\tilde{U}$        $.(C_d)$        $\tilde{U}$        $(C_d)$

$\hat{\otimes} \quad \hat{\circ} \quad (\mathbf{H}/\mathbf{P}) \quad \hat{\circ} \quad \hat{\circ} \quad \hat{\circ}$

.( Chilmeran , 1996 )

Ù Ù .(2)Ù , (P=20, 30)  
 Ø ( Noori & Hayawi, 1996 ; AL-Qasser, 1983 ; Acker, 1978) Ø  
 Ø Ø Ø Ø Ø

$$\begin{array}{ccccccc}
 & :(\mathbf{C}_d) & \emptyset & (\beta) & & \emptyset & -1 \\
 (\beta) & \tilde{\textcircled{O}} & \tilde{\textcircled{O}} & & \tilde{\textcircled{U}} & (\mathbf{C}_d) & \tilde{\textcircled{U}} \\
 (0.785-0.718) & & & & \tilde{\textcircled{U}} & & , \\
 \tilde{\textcircled{O}} & & .(4)\tilde{\textcircled{U}} & (H/P=0.2, p=30) & & & \tilde{\textcircled{U}} \\
 \tilde{\textcircled{O}} & & & (0.80-0.711) & & & \\
 (75^\circ-45^\circ) & (\beta)\tilde{\textcircled{U}} & & ,(H/P=0.16, \theta=60^\circ, p=30) & & & \tilde{\textcircled{U}}
 \end{array}$$

<u>:<b>(C<sub>d</sub>)</b></u>	$\emptyset$	-2
$\tilde{O}$	$\tilde{U}$	
$\tilde{O}$	$\tilde{O}$	
$\vdash$	$\vdash$	
		(SPSS Ver.10)
		$\tilde{U}$

Ő Ő Ő Ő Ő Ő Ő Ő Ő Ő  
 (θ=60°) (R=5) (P=30,20) (β=90°) (β=75°)  
 (Chilmeran, 1996)

$$\begin{array}{ccccccc}
 \tilde{O} & \tilde{O} & & U & \tilde{U} & .(3)U \\
 \tilde{O} & & & & & (H/P) \\
 \tilde{O} & & (H/P) & U & U & & \\
 \tilde{O} & \tilde{O} & & U & & & \\
 \\ 
 \tilde{O} & & & U & & & \\
 & & & (H/P) & & & \\
 Escande & ) & \tilde{O} & \tilde{O} & \tilde{O} & \tilde{O} & U \\
 & & & \tilde{U} & \tilde{O} & \tilde{O} & \\
 & & & & , & & \\
 & & & & \tilde{O} & \tilde{O} & \tilde{O} & \\
 & & & & .(Ramamurthy & Vo, 1994);(Sananes,1959) & & \\
 \end{array}$$

$$\begin{array}{ccccccc}
 \tilde{O} & (C_d) & \tilde{O} & \tilde{U} & U & (C_d) & U \\
 \tilde{O} & & & (H/P) & & & -1 \\
 \\ 
 ( P=10 ) & & ( \beta=75^\circ ) & & U & & \\
 \\ 
 \tilde{O} & (C_d) & \tilde{O} & \tilde{U} & ( \beta ) & & \\
 \\ 
 \tilde{O} & & & \tilde{U} & & U & U \\
 \tilde{O} & \tilde{O} & \tilde{U} & \tilde{O} & \tilde{U} & ( \theta=25^\circ ) & -4 \\
 \tilde{O} & & & & & .( \theta=60^\circ, 45^\circ, 30^\circ ) & \\
 \end{array}$$

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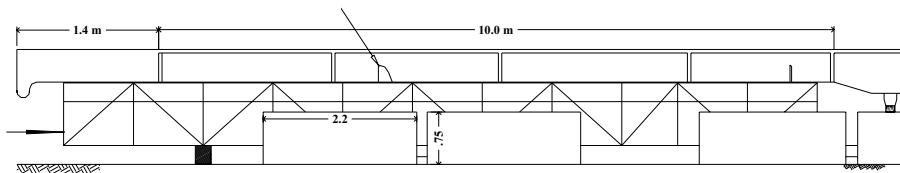
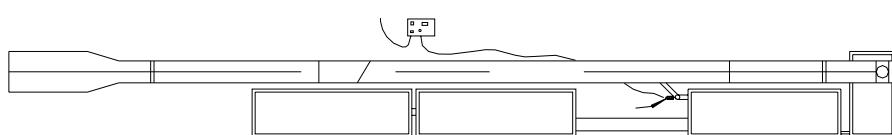
$\emptyset : (1)\emptyset$ 

Crest Height P(cm)	Crest Length L (cm)	Downstream angle ( $\beta$ )	Upstream angle ( $\alpha$ )	Series No.	Crest Radius R (cm)	Oblique angle ( $\theta$ )	Model No.	group No.
30 , 20 , 10	30	75°	75°	A	5	90° (Normal weir)	1 - 3	1
30 , 20 , 10	30	60°		B			4 - 6	
30 , 20 , 10	30	45°		C			7 - 9	
30 , 20 , 10	34.6	75°	75°	A	5	60°	10 - 12	2
30 , 20 , 10	34.6	60°		B			13 - 15	
30 , 20 , 10	34.6	45°		C			16 - 18	
30 , 20 , 10	42.424	75°	75°	A	5	45°	19 - 21	3
30 , 20 , 10	42.424	60°		B			22 - 24	
30 , 20 , 10	42.424	45°		C			23 - 27	
30 , 20 , 10	60	75°	75°	A	5	30°	28 - 30	4
30 , 20 , 10	60	60°		B			31 - 33	
30 , 20 , 10	60	45°		C			34 - 36	
30 , 20 , 10	70.98	75°	75°	A	5	25°	37 - 39	5
30 , 20 , 10	70.98	60°		B			40 - 42	
30 , 20 , 10	70.98	45°		C			43 - 45	

 $\emptyset : (2)\emptyset$ 

$\emptyset$										(θ°)	P (cm)
$\beta=45^\circ$			$\beta=60^\circ$			$\beta=75^\circ$					
Min.	Max.	H/P	Min.	Max.	H/P	Min.	Max.	H/P			
0.750	0.821	0.860	0.777	0.856	0.835	0.838	0.899	0.810	°90	10	
0.643	0.743	0.530	0.687	0.818	0.480	0.750	0.931	0.402	60°		
0.586	0.675	0.440	0.635	0.743	0.400	0.692	0.847	0.320	°45		
0.466	0.553	0.405	0.514	0.649	0.300	0.584	0.671	0.340	°30		
0.453	0.567	0.300	0.473	0.586	0.300	0.516	0.632	0.310	°25		
0.711	0.758	0.400	0.747	0.809	0.404	0.790	0.850	0.395	°90	20	
0.599	0.711	0.265	0.639	0.782	0.230	0.709	0.871	0.210	60°		
0.554	0.651	0.210	0.602	0.704	0.218	0.649	0.795	0.215	°45		
0.438	0.522	0.205	0.485	0.617	0.155	0.556	0.649	0.150	30°		
0.424	0.530	0.150	0.447	0.558	0.155	0.486	0.584	0.170	25°		
0.664	0.743	0.233	0.709	0.790	0.240	0.73	0.825	0.237	90°	30	
0.586	0.693	0.160	0.619	0.759	0.155	0.675	0.852	0.137	60°		
0.531	0.636	0.145	0.588	0.689	0.145	0.637	0.785	0.103	45°		
0.427	0.507	0.143	0.474	0.600	0.123	0.536	0.639	0.103	30°		
0.412	0.498	0.107	0.429	0.548	0.100	0.475	0.567	0.127	25°		

(2-1)		(2) ( $\beta=90^\circ$ )	(1) ( $\beta=75^\circ$ )	H/P	p(cm)	$\emptyset$ ( $\theta$ )
$\Delta Cd$ (%)		$\emptyset$ (Cd)	(Cd) $\emptyset$			
-24.11	0.591	0.7335	0.14	30	90°	
-7.63	0.695	0.748	0.16			
-27.71	0.599	0.765	0.18			
-29.00	0.607	0.783	0.2			
-30.47	0.617	0.805	0.22			
-35.04	0.585	0.790	0.28			
-36.22	0.588	0.801	0.3			
-37.16	0.592	0.812	0.32			
-38.32	0.595	0.823	0.34			
-39.30	0.598	0.833	0.36			
-19.01	0.710	0.845	0.14	30	60°	
-11.42	0.718	0.800	0.16			
-6.59	0.713	0.760	0.18			
-1.41	0.71	0.720	0.2			
0.00	0.706	0.706	0.22			
-24.66	0.734	0.915	0.18	20		
-20.90	0.732	0.885	0.20			
-17.65	0.731	0.860	0.22			
-14.35	0.7311	0.836	0.24			
-10.58	0.7325	0.810	0.26			



$\dot{U}$  :

